ROBUST SECOND ORDER SLIDING MODE CONTROL OF DOUBLY-FED INDUCTION GENERATOR FOR WIND ENERGY CONVERSION SYSTEM

Youcef DJERIRI
Department of Electrical Engineering, Faculty of Electrical Engineering
Djillali Liabes University, Intelligent Control and Electrical Power Systems Laboratory, PO Box 89, Sidi Bel-Abbes, 22000, Algeria
E-mail: youcef.djeriri@univ-sba.dz

ABSTRACT
This paper presents a robust nonlinear control strategy based on second-order continuous sliding mode control called Super-Twisting Sliding Mode Control (ST-SMC) strategy of a doubly-fed induction generator (DFIG) integrated into a Wind Energy Conversion System (WECS). The Conventional Sliding Mode Control (C-SMC) strategy has a significant drawback, which is the chattering phenomenon, caused by the discontinuous control signal. The proposed ST-SMC technique based on second-order continuous sliding mode control reduces powers, currents, and torque ripples, while maintaining the advantages of the conventional method (C-SMC) such as the robustness against parametric variations of the DFIG. Simulation results show the effectiveness of the proposed ST-SMC strategy in reducing the chattering effect comparatively to the C-SMC one.

Keywords: Wind energy, DFIG, second order sliding mode control, chattering phenomenon, robustness.

1. INTRODUCTION
Wind energy is the most promising renewable source of electrical power generation for the future. Many countries promote wind power technology through various national programs and market incentives. Wind energy technology has evolved rapidly over the past three decades with increasing rotor diameters and advanced power electronics to allow operation at the variable speed [1].

Since twenties years, the concept of the variable speed wind turbine (VSWT) equipped with a doubly fed induction generator (DFIG) has received increasing attention due to its noticeable advantages over other wind turbine concepts. In the DFIG concept, the stator is usually connected directly to the three-phase grid; the rotor is also connected to the grid but via a transformer and two back-to-back converters. Usually, the rotor-side converter (RSC) controls the active and reactive powers and the grid side converter (GSC) controls the DC-link voltage and ensures operation of the converter at a unity power factor [2]. This arrangement provides the flexibility of operation in sub and super-synchronous speeds in both generating and motoring modes (±30% around the synchronous speed). The power inverter needs to handle a fraction (20-30%) of the total power to achieve full control of the generator [3].

In the literature, many control methods have been suggested to control DFIG's powers, such as the vector control technique based on traditional Proportional Integral (PI) controllers, due to their simple implementation [4]. However, the classical PI controller may not give satisfactory performance against variations of DFIG parameters [4],[5].

In recent years, many robust control techniques have been proposed in the literature to improve the operation performances of the DFIG. The sliding mode control (SMC) strategy has been widely used for robust control of nonlinear systems. Sliding mode control, based on the theory of variable structure systems (VSS), has attracted a lot of research on control systems for the last two decades. It achieves robust control by adding a discontinuous control signal across the sliding surface, satisfying the sliding condition. However, this type of control has an essential disadvantage, which is the chattering problem caused by the discontinuous control action [6].

In this paper, the Super-Twisting Sliding Mode Control (ST-SMC) has been introduced to overcome the chattering problem while keeping the convergence properties in finite time and robustness of Conventional Sliding Mode Control (C-SMC). In ST-SMC approach, the discontinuous term no longer appears directly in the expression of the synthesized control but in one of its higher derivatives, which has the merit of reducing chattering [7].

Finally, simulation results show that the proposed ST-SMC strategy effectively reduces the powers and currents ripples as well as minimal mechanical stress on the rotor of the DFIG, compared to the C-SMC strategy.

2. MODELING OF THE DFIG

The equivalent circuit of the DFIG in the synchronous reference frame rotating at the angular synchronous speed \( \omega_s \) is depicted in Fig.1.

The model of the DFIG in the synchronous \( d-q \) reference frame is given by the following equations: Stator voltage components:

\[
\begin{align*}
V_{ds} &= R_s I_{ds} + \frac{d}{dt} \psi_{ds} - \omega_s \psi_{qs} \\
V_{qs} &= R_s I_{qs} + \frac{d}{dt} \psi_{qs} + \omega_s \psi_{ds}
\end{align*}
\]  

(1)
Rotor voltage components:

\[
\begin{align*}
V_{dr} &= R_d I_{dr} + \frac{d}{dt} \psi_{dr} \ - (\omega_s - \omega_r) \psi_{dq} \\
V_{qr} &= R_q I_{qr} + \frac{d}{dt} \psi_{qr} + (\omega_s - \omega_r) \psi_{dr}
\end{align*}
\]

Stator flux components:

\[
\begin{align*}
\psi_{ds} &= L_s I_{ds} + L_m I_{dr} \\
\psi_{qs} &= L_s I_{qs} + L_m I_{qr}
\end{align*}
\]

Rotor flux components:

\[
\begin{align*}
\psi_{dr} &= L_s I_{ds} + L_m I_{ds} \\
\psi_{qr} &= L_s I_{qs} + L_m I_{qs}
\end{align*}
\]

DFIG electromagnetic torque:

\[
T_{em} = \frac{3}{2} \frac{L_m}{L_s} (\psi_{ds} I_{dr} - \psi_{qs} I_{qr})
\]

Mechanical equation:

\[
T_i = T_{em} + J \frac{d\Omega_r}{dt} + f_r \Omega_r
\]

Replacing the stator currents by their expressions given in (11), the equations below are expressed by:

\[
\begin{align*}
P_s &= \frac{3}{2} V_s I_{qs} \\
Q_s &= \frac{3}{2} V_s (\psi_{ds} - L_m I_{dr})
\end{align*}
\]

The electromagnetic torque is as follows:

\[
T_{em} = -\frac{3}{2} \frac{L_m}{L_s} \psi_{qs} I_{qr}
\]

3. CONVENTIONAL SLIDING MODE CONTROL OF DFIG

In order to control the stator active and reactive powers and for a relative degree equal to 1, the expression of the surface has the form:

\[
\begin{align*}
S_i &= P_i^* - P_s \\
S_q &= Q_i^* - Q_s
\end{align*}
\]

Where: \(P_i^*\) and \(Q_i^*\) are successively the references of the active and reactive powers.

The derivative of the surface is:

\[
\begin{align*}
\dot{S}_1 &= P_i^* - \dot{P}_s \\
\dot{S}_2 &= Q_i^* - \dot{Q}_s
\end{align*}
\]

We replace the derivatives of the active and reactive powers by their expressions in (16), we obtain:

\[
\begin{align*}
\dot{S}_1 &= P_i^* + \frac{3}{2} V_s \frac{L_m}{L_s} \left( f_s + \frac{V_{qr}}{\sigma L_r} \right) \\
\dot{S}_2 &= Q_i^* + \frac{3}{2} V_s \frac{L_m}{L_s} \left( f_i + \frac{V_{dr}}{\sigma L_r} \right)
\end{align*}
\]
Where:

\[
\begin{align*}
    f_1(x) &= -\frac{R_s}{L_s} I_d + g \omega_s I_q \\
    f_2(x) &= -g \omega_s I_d - \frac{R_s}{L_s} I_q - g L_m V_s
\end{align*}
\]  

(18)

Where: \( \sigma = 1 - \left( \frac{L_m}{L_s} \right) \) is the leakage factor, and \( g \) is the slip of the induction machine.

According to the sliding mode theory, we replace respectively \( V_d \) and \( V_q \) by \( V_{d0} + V_{d0}^a \) and \( V_{q0} + V_{q0}^a \) in (17), we have:

\[
\begin{align*}
    V_d^a &= \frac{2}{3} \frac{L_s}{V_s} L_m^* P_{r} - \sigma L_s f_2 \\
    V_q^a &= \frac{2}{3} \frac{L_s}{V_s} L_m^* Q_{r} - \sigma L_s f_1
\end{align*}
\]  

(19)

By definition, the discontinuous terms \( V_d^a \) and \( V_q^a \) are given by [10]:

\[
\begin{align*}
    V_d^a &= -k_1 \text{sign} (S_1) \\
    V_q^a &= -k_2 \text{sign} (S_2)
\end{align*}
\]  

(20)

So that the control system becomes asymptotically stable, the gains \( k_1 \) and \( k_2 \) must be positives [11]. The chosen values of \( k_1 \) and \( k_2 \) are 90000.

The Fig. 2 shows the block diagram of the conventional sliding mode control of the DFIG.

4. SUPER-TWISTING SLIDING MODE CONTROL

4.1. General Principle of ST-SMC

Higher-order sliding modes were introduced by Emelyanov [12] and Levantovsky [13]. They represent an extension of the first order sliding modes to a higher degree. This generalization retains the main characteristic in terms of robustness than that of conventional sliding modes. They also reduce their main disadvantage: the chattering effect in the vicinity of the sliding surface. The extension of first-order sliding modes to higher-order sliding modes is characterized by the choice of discontinuous control acting not on the sliding surface but on its higher derivatives [7], [14].

The purpose of this type of controllers is to generate a second-order sliding regime on a surface \( S \) by the cancellation of \( S \) itself as well as its derivative in a finite time \( S = S = 0 \). The main feature of this strategy is that the discontinuous part appears on the derivative of the control \( \dot{u} \). Finally, when one calculates the control of the system \( u = \int \dot{u} \), it becomes continuous thus limiting the chattering problem [14], [15].

The Super-Twisting algorithm is one of the most widely used second-order sliding mode algorithms. This algorithm only applies to systems that have one relative degree [16].

The convergence of this algorithm is governed by rotations around the origin of the phase plane (also called Twisting), as shown in Fig.3. The control law of Super-Twisting is formed of two parts. The first \( u_1 \) is defined by its derivative with respect to time, while the second \( u_2 \) is continuous and according to the sliding variable. For a real sliding mode, the control law will be given by [17]:

Fig. 2 Block diagram of the conventional sliding mode control of the DFIG
Then the proposed control law applied in this paper is given by the following equation \[7\], \[14\]:

\[
\begin{align*}
    u(t) &= -l_s \left| S \right|^{0.5} \text{sign}(S) + v_1(t) + v_2(t) \\
    v_1(t) &= -K \text{sign}(S) \\
    v_2(t) &= -l_s \left| S \right|^{0.5} \text{sign}(S)
\end{align*}
\]  

Where: \( v \) is defined by (23) and (24) and the scalars \( a_1, a_2,..., a_n \) satisfy (25). In addition, \( l_1, l_2,..., l_n \) are scalars coefficients defined such that the \( n \)th order polynomial \( p^n + l_1 p^{n-1} + ... + l_n p + l_0 \) is Hurwitz.

The main problem of the control is to determine input function \( u = f(y, \dot{y}) \) whereas it can drive the system trajectories to the initial point \( y = \dot{y} = 0 \) of the phase plane in a limited time \[7\], \[20\]. The input \( u \) is defined as a new state variable and the switching control is applied to its time derivative \( \dot{u} \). The output \( y \) is controlled by an ST-SMC controller with sliding variable \( S = y^* - y \).

This control strategy does not use the derivative of the sliding variable. As show in (26) and (28), the adequate condition for convergence to the sliding surface and for stability that the gains are large enough \[7\], \[14\], \[19\], \[20\].

\[
\begin{align*}
    A &\geq A_m, \quad B \geq B_m, \quad k_1 \geq \frac{4 A_m B_m (k_1 + A_m)}{B_m (k_1 - A_m)}
\end{align*}
\]  

Where: \( A_m \geq |A| \) and \( B_m \geq B \geq B_m \) are the superior and inferior bounds of \( A \) and \( B \), respectively, in the second derivative of \( y \).
Fig. 4. Block diagram of the super-twisting sliding mode control of the DFIG

The Fig. 4 shows the block diagram of the super-twisting sliding mode control of the DFIG.

5. SIMULATION RESULTS AND DISCUSSION

In this section, the C-SMC and the ST-SMC control strategies of 1.5MW DFIG (see Table 1 in appendix) are tested by simulation under MATLAB/SIMULINK software. Both techniques are compared according to three criteria:
1- References tracking test at variable wind speed.
2- Robustness test against the parameters variations of the DFIG at fixed wind speed.
3- Power quality analysis (chattering effect).

5.1. References tracking test

In this test, the wind turbine is driven by a variable wind speed with an average value of 8.2 m/s (Fig. 5.a). The reference active power is generated by the MPPT (Maximum Power Point Tracking) strategy and the reactive power reference is kept at zero in order to guarantee a unit power factor on the stator side of the DFIG.

The Fig. 5 presents the simulation results of the classical sliding mode control technique (C-SMC) of the DFIG.

Fig. 5 Simulation results of C-SMC of DFIG (references tracking test)

The Fig. 5.b shows a very fast response of the active power, where it follows perfectly its reference generated by the MPPT strategy with a negligible error in sub and super-synchronous mode operations of DFIG. The reactive power is maintained at its reference equal to zero (Fig. 5.c), in order to achieve a unit power factor (FP = 1) on the stator side of the DFIG. These simulation results show the high performances of C-SMC strategy of DFIG.
The Fig. 6 presents the simulation results of the super-twisting sliding mode control (ST-SMC) strategy of the DFIG at the same simulation conditions as the previous technique (C-SMC).

![Graph of active power response](image1)

(a) : active power response

![Graph of reactive power response](image2)

(b) : reactive power response

**Fig. 6** Simulation results of ST-SMC of DFIG (references tracking test)

The results in Fig. 6 show clearly the effectiveness of the ST-SMC strategy in the separate control of the active and reactive stator powers of the DFIG. These latter perfectly follow their reference values with a very satisfactory performance.

### 5.2. Robustness test

In order to test the robustness of the tow control strategies C-SMC and ST-SMC of the DFIG, we also studied the influence of parameters variations of the generator on the performances of these last control strategies.

To realize this test, we increase the rotor resistance ($R_r$) by 100% of its nominal value (case of warming-up of rotor windings) and decrease the mutual inductance ($L_m$) by 50% of its nominal value (case of inductances saturation), at the same time.

Fig. 7 and 8 show the active power, the reactive power, the stator current and the rotor current responses of DFIG for the C-SMC strategy and the proposed ST-SMC scheme respectively, where the wind turbine is driven at fixed wind speed of 12 m/s.

In this test, the reactive power reference enabled the WECS (Wind Energy Conversion System) to have a negative reactive power (capacitive operating mode) or positive (inductive operating mode). On the other hand, the active power is kept negative, this means that the WECS always generates the active power towards the electrical grid.

![Graph of active power response](image3)

(a) : active power response

![Graph of reactive power response](image4)

(b) : reactive power response

![Graph of stator current response](image5)

(c) : stator current response

![Graph of rotor current response](image6)

(d) : rotor current response

**Fig. 7** Simulation results of the robustness test against parameters variations of DFIG for C-SMC
5.3. Harmonics analysis test

This third test is about chattering phenomenon associated to the sliding mode techniques. In this test the Total Harmonic Distortion (THD) of the stator current of the DFIG is measured by using the Fast Fourier Transform (FFT) method for both C-SMC and ST-SMC control schemes.

Fig. 9 shows the results obtained from the spectral analysis of a phase of the stator current.

The Fig. 9.a shows a total harmonic distortion rate equal to 9.56%, this is due to the chattering phenomenon, which represents a big problem of the conventional sliding mode control (C-SMC), it can cause harmful effects on the generator and could damage the mechanical components of a system because the discontinuous control signal [14], [20], [21], [22].
The Fig. 9.b shows that the proposed ST-SMC strategy guarantees a better quality of the stator current waveform injected to the grid, where the total harmonic distortion (THD) rate is only 6.03%.

6. CONCLUSION

In this paper there have been presented two robust nonlinear control strategies, C-SMC and ST-SMC, allowing independent control of the active and reactive stator powers of the DFIG, driven by a variable speed wind turbine. The performances obtained by these two control strategies are very satisfactory even in the presence of parameters variations as shown by the trajectory tracking and the fast convergence of the measured variables towards their desired references. However, because of the discontinuous component, C-SMC technique has a higher harmonic distortion level on the output variables, compared to the ST-SMC scheme. Finally, from the simulation results, it can be said that the proposed ST-SMC control strategy of DFIG is a very simple robust control algorithm which has the advantage of being easily for a real time implementation.

APPENDIX

Table 1 Wind energy conversion system parameters

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Rated Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rated power, ( P_r )</td>
<td>1.5</td>
<td>MW</td>
</tr>
<tr>
<td>Blade radius, ( R )</td>
<td>35.25</td>
<td>m</td>
</tr>
<tr>
<td>Number of blades</td>
<td>3</td>
<td>-</td>
</tr>
<tr>
<td>Gearbox ratio, ( G )</td>
<td>90</td>
<td>-</td>
</tr>
<tr>
<td>Total moment of inertia, ( J )</td>
<td>1000</td>
<td>kg.m²</td>
</tr>
<tr>
<td>Viscous friction coefficient, ( f_r )</td>
<td>0.0024</td>
<td>N.m.s⁻¹</td>
</tr>
<tr>
<td>Nominal wind speed, ( v )</td>
<td>12</td>
<td>m/s</td>
</tr>
<tr>
<td>Stator rated voltage, ( V_s )</td>
<td>398/690</td>
<td>V</td>
</tr>
<tr>
<td>Rotor rated voltage, ( V_r )</td>
<td>225/389</td>
<td>V</td>
</tr>
<tr>
<td>Rated current, ( I_r )</td>
<td>1900</td>
<td>A</td>
</tr>
<tr>
<td>Stator rated frequency, ( f )</td>
<td>50</td>
<td>Hz</td>
</tr>
<tr>
<td>Stator inductance, ( L_s )</td>
<td>0.0137</td>
<td>H</td>
</tr>
<tr>
<td>Rotor inductance, ( L_r )</td>
<td>0.0136</td>
<td>H</td>
</tr>
<tr>
<td>Mutual inductance, ( L_m )</td>
<td>0.0135</td>
<td>H</td>
</tr>
<tr>
<td>Stator resistance, ( R_s )</td>
<td>0.012</td>
<td>Ω</td>
</tr>
<tr>
<td>Rotor resistance, ( R_r )</td>
<td>0.021</td>
<td>Ω</td>
</tr>
<tr>
<td>Number of pair of poles, ( p )</td>
<td>2</td>
<td>-</td>
</tr>
<tr>
<td>Slip range, ( g )</td>
<td>-0.3 to 0.3</td>
<td>-</td>
</tr>
</tbody>
</table>

REFERENCES


Robust Second-Order Sliding Mode control of Doubly-Fed Induction Generator for Wind Energy Conversion System


Received June 2, 2020, accepted June 26, 2020

**BIOGRAPHY**

Youcef Djeriri was born in Algeria in 1984. He received the PhD degree in Electrical Engineering from the Electrical Engineering Faculty of Djillali Liabes University at Sidi Bel-Abbes, Algeria, in 2015. He is a member of Intelligent Control & Electrical Power Systems – ICEPS – research laboratory. His research interests are in the field of robust, advanced and intelligent control methods of AC drives associated with power electronic converters for the renewable energy applications. E-mail: youcef.djeriri@univ-sba.dz