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#### ABSTRACT

The induction heating phenomenon depends on various factors, making the problem highly nonlinear. The mathematical analysis of this problem in most cases is very difficult and it is reduced to simple cases. Other knowledge of induction heating systems is generated in production environments, but these trial-error procedures are long and expensive. The numerical models of induction heating problem are another approach to reduce abovementioned drawbacks. This paper deals with the simulation model of induction heating system in COMSOL Multiphysics is created. The equivalent inductance and equivalent resistance of induction coil – workpiece coupling during heating process and temperature change for different parameters of AC current flowing through induction coil is obtained. In model, nonlinear electromagnetic and thermal properties of workpiece material are included. The simulation model provides essential information about processes ongoing in heated material. In order to verify the simulation model, the experimental measurements are made.

Keywords: COMSOL Multiphysics, induction heating, nonlinear material, numerical simulation

# 1. INTRODUCTION

The induction heating (IH) is unique, non – contact technique of heating electrically conductive materials. As its name implies, this technique relies on eddy currents that are internally induced in heating material. These eddy currents flow in electrically conductive material causing the primary mechanism of heat dissipation due to Joule's heat. This mechanism of heat generation is present in every electrically conductive material even non-magnetic one. The second mechanism of heat generation in workpiece is related with hysteresis losses and it is only present in magnetic materials [1].

The design of IH system includes knowing the processes ongoing in workpiece and induction coil. This includes the electromagnetic phenomena such as non-uniform distribution of magnetic flux density and current density in the workpiece and the coil, coupling between the workpiece and induction coil, the shape of the coil and workpiece. Heat generation, heat transfer in material and heat transfer between the material and external environment are other factors to be considered in induction heating phenomenon.

Abovementioned processes are all related to physical properties of material to be heated. These properties include the electromagnetic and thermal properties of material and they are highly depended on its temperature. The amount of heat generated in workpiece depends on the magnitude of electric current flowing through the coil and heating depth depends on its frequency.



Fig. 1 IH system

Considering the previous facts, the IH phenomenon is a complex problem, thus numerical simulations seem to be a useful tool for the design and the investigation of IH systems [4].

The basic IH system consists of source of AC current, induction coil a workpiece itself (Fig.1). In order to design the source of AC current, the equivalent resistance ( $R_{eq}$ ) and equivalent inductance ( $L_{eq}$ ) of induction coil – workpiece coupling needs to be estimated based on the series model of this coupling (Fig. 2) [5].



Fig. 2 Series model of induction coil – workpiece coupling

In this paper, the model of induction heating using finite elements method of solution is introduced which considers non-linear properties of heated material. This model allows observing the relations that are present in workpiece and induction coil during the heating process.

The laboratory model of converter is developed and experimental measurements of temperature are compared with simulation results.

# 2. MATHEMATICAL MODEL OF IH

The induction heating phenomenon consists of coupled problem combining the electromagnetic problem and thermal problem including the radiation and convective transition considering the material properties [4].

## 2.1. Electromagnetic problem

The problem of electromagnetic analysis on a macroscopic level is that of solving Maxwell's equations and constitutive relationships subject to certain boundary conditions. For general time – varying fields, Maxwell's equation can be written as [3], [8]:

$$\nabla \times \mathbf{H} = \mathbf{J} + \frac{\partial \mathbf{D}}{\partial t} \tag{1}$$

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t} \tag{2}$$

 $\nabla \mathbf{.D} = \rho \tag{3}$ 

$$\nabla \mathbf{.B} = 0 \tag{4}$$

where:  $\mathbf{H}$  – magnetic field intensity,  $\mathbf{J}$  – current density,  $\mathbf{B}$  – magnetic flux density,  $\mathbf{E}$  – electric field intensity,  $\mathbf{D}$  – electric flux density,  $\rho$  – electric charge density.

To obtain a closed system, the equations include constitutive relationships that describe the macroscopic properties of the medium:

 $\mathbf{D} = \varepsilon_0 \varepsilon_r \mathbf{E} \tag{5}$ 

 $\mathbf{B} = \mu_0 \mu_r \mathbf{H} \tag{6}$ 

$$\mathbf{J} = \boldsymbol{\sigma} \mathbf{E} \tag{7}$$

where:  $\varepsilon_0$  – vacuum permittivity,  $\varepsilon_r$  – relative permittivity,  $\mu_0$  – vacuum permeability,  $\mu_r$  – relative permeability,  $\sigma$  – electrical conductivity.

The simulation model of induction heating created in 2D axisymmetric domain is shown in Fig. 3. The solution domain  $\Omega$  is divided into three subdomains: air ( $\Omega_3$ ), coil ( $\Omega_2$ ) and workpiece domain ( $\Omega_1$ ). For the workpiece a bolt M12x60 mm made of carbon steel was chosen.



Fig. 3 IH model in COMSOL Multiphysics

The material of subdomain  $\Omega_1$  is medium carbon steel. Both domains  $\Omega_1$  and  $\Omega_2$  are surrounded with nonconductive air region  $\Omega_3$ . Equations for this particular problem for frequency – transient analysis can be written as follows [3]. Subdomain  $\Omega_1, \Omega_3$ :

$$(j\omega - \omega^2 \varepsilon_0 \varepsilon_r) \mathbf{A} + \nabla \times (\mu_0^{-1} \mu_r^{-1} \mathbf{B}) = \mathbf{J}_e$$
(8)

$$\mathbf{B} = \nabla \times \mathbf{A} \tag{9}$$

where: j – imaginary unit,  $\omega$  – angular frequency, **A** – magnetic vector potential, **J**<sub>e</sub> – current density.

Subdomain 
$$\Omega_2$$
:

$$(j\omega - \omega^2 \varepsilon_0 \varepsilon_r) \mathbf{A} + \nabla \times \mathbf{H} = \mathbf{J}_{\mathbf{e}}$$
(10)

$$\int_{\Omega} \mathbf{J}_i \mathbf{\Phi} dS = I_{coil} \tag{11}$$

$$\mathbf{J}_{\mathbf{e}} = \frac{\sigma V_i}{2\pi r} \mathbf{\Phi} \tag{12}$$

$$V_{coil} = \sum V_i \tag{13}$$

where:  $\Phi$  – magnetic flux,  $I_{coil}$  – coil current,  $V_i$  – voltage of one turn of the coil,  $V_{coil}$  – voltage of the coil.

Boundary 
$$\Gamma_3$$
:

$$\mathbf{n} \times \mathbf{A} = 0 \tag{14}$$

where: **n** – outward normal from medium.

#### 2.2. Thermal problem

The fundamental law describing all heat transfer is the first law of thermodynamics. It is commonly referred as the principle of conservation energy. In induction heating, all three modes of heat transfer – conduction, convection and radiation are present [3].

The law that describes heat transfer by conduction is known as Fourier's law [1]:

$$q_{cond} = -k\nabla T \tag{15}$$

where:  $q_{cond}$  – heat flux by conduction, k – thermal conductivity, T – temperature.

In this mode of heat transfer, heat is transferred from high – temperature regions towards low – temperature region.

On the other hand heat transfer by convection carries out only in gas or fluid and it is described by the Newton's law as follows [1]:

$$q_{conv} = -h(T_{and} - T) \tag{16}$$

where:  $q_{conv}$  – heat flux by convection, h – convection heat transfer coefficient,  $T_{amb}$  – ambient temperature.

This law describes the heat transfer between the surface of the heated worpiece and ambient area. The heat transfer rate is proportional to the temperature difference and heat transfer coefficient.

Last mode of heat transfer is known as heat radiation. The heat is transferred from the hot surface of the

workpiece to the ambient area including nonmaterial region (vacuum). Heat transfer by radiation takes place through the transport of photons. Participating media absorb, emit and scatter photons. Opaque surface absorb or reflect them [3]. The basic law that governs this mode of heat transfer is known as Stefan – Boltzmann's law [1]:

$$q_{rad} = \mathcal{E}(T_s^4 - T_{amb}^4) \tag{17}$$

where:  $q_{rad}$  – radiation loss density,  $\varepsilon$  – surface emissivity,  $\sigma$  – Stefan – Boltzmann constant,  $T_s$  – surface temperature.

According to previous modes of heat transfer, the equations for subdomains and boundaries can be written as follows [3]:

Subdomain  $\Omega_1$ :

$$\rho C_p \frac{\partial T}{\partial t} + \nabla (-k\nabla T) = Q$$
(18)

$$Q = Q_{m} + Q_{ml} \tag{19}$$

where:  $C_p$  – heat capacity,  $\rho$  – density, Q – heat sources other than viscous heating,  $Q_{rh}$  – resistive losses,  $Q_{ml}$  – magnetic losses.

Boundary  $\Gamma_3$ :

$$-\mathbf{n}.(-k\nabla T) = h(T_{ext} - T)$$
(20)

$$-\mathbf{n}(-k\nabla T) = \varepsilon\sigma(T_{anb}^{4} - T^{4})$$
(21)

# 2.3. Electromagnetic and thermal properties of workpiece material

Electromagnetic and heat transfer phenomenon are highly interrelated because the physical properties of heated metals. These properties of metals are nonlinear functions of magnetic field intensity, temperature, chemical composition and other factors [1].

This mathematical model considers the main properties that have the most significant impact on induction heating technology. These properties are: relative permeability  $\mu_r$ , electric resistivity  $\rho$ , thermal conductivity k and heat capacity  $C_p$ . Values of these properties used in simulation for carbon steel depending on temperature are listed in Tab.1. The Curie temperature was set to  $T_c = 740$  °C.

It should be noted that surface emissivity  $\varepsilon$  and convection heat transfer coefficient *h* are temperature depended as well (other factors that influence  $\varepsilon$  and *h* are: viscosity, surface condition, etc...), but in this model these properties as well as conductivity of copper of induction coil (subdomain  $\Omega_2$ ) remain constant during heating process.

The value of emissivity was set to  $\varepsilon = 0, 75$ , convection heat transfer coefficient is h = 15 W.m<sup>-2</sup>.K<sup>-1</sup> and value of electric conductivity of the coil is  $\sigma = 5, 99.10^7$  S.m<sup>-1</sup>.

 Table 1
 Electromagnetic and thermal properties of medium carbon steel depending on temperature

Т	k	$C_p$	ρ	$\mu_r$
[K]	[W/(m.K)]	[J/(kg.K)]	[Ω.m]	[-]
293	52	450	1,70.10-7	218
373	51	490	2,32.10-7	-
473	-	-	3,10.10-7	-
573	46	570	4,10.10-7	202
673	-	-	5,05.10-7	-
773	38	680	-	-
873	-	-	7,72.10-7	164
973	30	-	9,35.10-7	81
1013	-	-	1,03.10-6	27
1073	-	-	1,13.10-6	1
1273	27	570	-	1
1473	27	570	1,23.10-6	1

# 3. SIMULATION RESULTS

The simulation results of induction heating model for coil current  $I_{max} = 50$  A and frequency f = 100 kHz are shown in Fig. 4. The simulation time was set to 10 min. The maximum temperature reached is 611 °C.



Fig. 4 Temperature of workpiece after 600 s of heating

The surface temperature of workpiece (shown in Fig. 3) is depicted in Fig. 5.



Fig. 5 Surface temperature of workpiece during heating process for  $I_{max} = 50$  A and f = 100 kHz

The  $R_{eq}$  and  $L_{eq}$  of coil - worpiece model is shown in Fig. 6 and Fig. 7, respectively.



Fig. 6 Equivalent inductance during heating process for  $I_{max} = 50$  A and f = 100 kHz

The initial value of  $L_{eq}$  is 1.14 µH. After 600 s the value settled down to  $L_{eq} = 1.20$  µH.



**Fig. 7** Equivalent resistance during heating process for  $I_{max} = 50$  A and f = 100 kHz

The value of  $R_{eq}$  has similar graph as for  $L_{eq.}$  In this case the initial value is  $R_{eq} = 0.064 \ \Omega$  and maximum value reached is  $R_{eq} = 0.091 \ \Omega$ .

#### 4. EXPERIMENTAL RESULTS

Considering the previous results the real induction coil and source of AC current were built. Using the simulation results of  $R_{eq}$  and  $L_{eq}$  the frequency of resonant circuit was calculated, since the converter used in experimental measurements utilizes an LCL resonant circuit [6], [7]. During the heating of workpiece  $L_{eq}$  and  $R_{eq}$  varies, thus the resonant frequency range needs to be calculated.

Calculated resonant frequency of this circuit varies within range  $f_r = 103.3 - 105.2$  kHz.

The experimental measurement of temperature for above-mentioned frequency range and coil current of  $I_{max} = 50$  A is shown in Fig. 8.



Fig. 8 Comparison between simulation and experimental measurement for  $I_{max} = 50$  A

The measuring point is again depicted in Fig. 3. The difference between the simulation and experimental measurement is shown in Fig. 9.



Fig. 9 Relative error between simulation and experimental measurement

The relative error in dynamic states reached value of 61 %. This could be caused by constant value of surface emissivity and convection heat transfer coefficient. Another reason is that frequency of measurement AC current varied within range 103.3 - 105.2 kHz and frequency used in simulation was set to 100 kHz. On the other hand, in steady – state, error is approximately 5%.

In the Fig. 10 the induction coil used in experimental measurements is shown.



Fig. 10 Real induction coil

## 5. CONCLUSIONS

In this paper the simulation model of induction heating considering the non-linear properties of metal is developed. The simulation model was compared with experimental results. The experimental measurements show that chosen approach is acceptable for designing systems that utilize induction heating technology.

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